

Reading Assignment for The Physics of Galaxy Clusters (Winter Term 2022/23)

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in preparation of lecture 9

Next lecture Dec 14, 2022, 14:15

Please read and work through the script, covering the following topics:

Start on pg. 77 with *3.2 Radiative Physics* and continue with

3.2.1 Radiative Cooling

3.2.2 Cooling versus Heating

3.2.3 Feedback by Supernovae

3.2.4 Feedback by Active Galactic Nuclei

I prepared the following questions that should help you to understand the topics. Please read a topic first, think about it and then work through my set of questions on this topic. Some questions are going beyond what you have read in the lecture notes (indicated by *Bonus* questions). I do not expect you to answer these questions as well, but I would like you to start thinking about them and they will certainly be the starting point for our next lecture. Ideally you can come up with many more questions yourself. **If you have problems with a derivation or if something is unclear, please email me those points well before the lectures!**

• Radiative cooling

- Explain the physics of bremsstrahlung emission and motivate the main dependencies in the bremsstrahlung emissivity, $j \propto n^2 \sqrt{k_B T}$ via physical arguments.
- Calculate the radiative cooling time t_{cool} of the X-ray-emitting gas for the core region of a cool-core cluster ($n_e = 3 \times 10^{-2} \text{ cm}^{-3}$ and $k_B T = 1 \text{ keV}$) and non-cool core cluster ($n_e = 3 \times 10^{-3} \text{ cm}^{-3}$ and $k_B T = 4 \text{ keV}$). Compare your result to the age of the universe and discuss it.
- Discuss qualitatively, what happens to t_{cool} at larger radii. Where in a cluster is cooling time minimized?
- Rewrite the cooling time 1. as a function of entropy and temperature and 2. as a function of entropy and cluster mass (using the ideal temperature-mass scaling relation).

• Cooling versus heating

- Verify the expression for the X-ray luminosity of a cluster (Eqns. 3.189 and 3.190) with a beta profile

$$n(r) = n_0 \left[1 + \left(\frac{r}{r_c} \right)^2 \right]^{-3\beta/2}, \quad (1)$$

where $\beta = 2/3$ and 1.

- Why does the X-ray luminosity depend on the core radius and not the virial radius? Why does it depend on the value of the density in the center and not the average cluster density?

- How does the mass profile scale with radius at large radii for these two values of β ? Compare this to the mass profiles of the singular isothermal sphere and the NFW profile and recall our remarks about the applicability of the mass profiles at large radii of order the virial radius and beyond.
- The density distribution of a **cool core cluster** is characterized by a double beta profile,

$$n(r) = \sum_{i=1,2} n_i \left[1 + \left(\frac{r}{r_{c,i}} \right)^2 \right]^{-3\beta_i/2}. \quad (2)$$

Plot the density profile of this cluster as a function of radius in a double-logarithmic representation for $\beta_{1,2} = 1$, $(n_1, n_2) = (10^{-1}, 10^{-2}) \text{ cm}^{-3}$, and $r_{c,1}, r_{c,2} = (10, 100) \text{ kpc}$.

- Plot the cooling time as a function of radius in a double-logarithmic representation and assume a constant temperature of 2 keV. Use this to calculate the cooling radius for this cluster, which is the radius where the cooling time equals 1 Gyr.
- The density distribution of a **non-cool core cluster** obeys a single beta profile. If you drop the first term and only account for the second term (with subscripts 2), calculate the cooling radius (if there is one). Discuss your results in comparison to cool-core clusters and argue whether you also have a severe overcooling problem in a non-cool core cluster.

• Feedback by supernovae

- Explain the currently favoured scenarios for core-collapse and thermonuclear supernovae (SNe).
- How much energy per nucleon can be delivered by core-collapse SNe and by thermonuclear SNe to the ICM over its entire life time?
- Compare this energy input to the gravitational binding energy of a nucleon in our Milky Way (with circular velocity $v_{\text{gal}} = 220 \text{ km s}^{-1}$) and in a massive galaxy clusters (with velocity dispersion $\sigma_{\text{cluster}} = 1200 \text{ km s}^{-1}$) and discuss the thermodynamic impact of SNe in either system.

• Feedback by active galactic nuclei

- Estimate the mass of a supermassive black hole in a massive elliptical BCG with $M_{\star, \text{BCG}} \sim 10^{12} M_{\odot}$ using the stellar bulge-black hole mass relation. Why can we identify the bulge mass in this relation with the stellar mass of the elliptical galaxy?
- Estimate the released gravitational energy per nucleon of an AGN that accretes its own mass and adopt a radiative efficiency of $\eta \sim 0.1$. Use the supermassive black hole mass corresponding to a BCG galaxy with $M_{\star, \text{BCG}} \sim 10^{12} M_{\odot}$.
- Calculate the sound crossing time. Calculate the buoyant rise time and the time required to refill the volume as the bubble rises and express those in units of the sound crossing time.
- Calculate the work done by two AGN bubbles in one outburst and adopt the following properties of the AGN bubbles: $r_b = 20 \text{ kpc}$, $n_a = 10^{-2} \text{ cm}^{-3}$, $k_B T = 3 \text{ keV}$. Use this to calculate the AGN heating rate and compare this to the X-ray “cooling” luminosity in the lectures.
- Calculate the Schwarzschild radius for the supermassive black hole in M87 and compare this to the cooling radius of our cool core cluster characterized by the double beta profile in Eqn. (2). By how many orders of magnitude does this differ?

- Explain the physical challenges of self-regulated AGN feedback where gas accretion at the Schwarzschild radius regulates thermally unstable gas at the cooling radius. Which property of AGN jets could make this possible?