Shocks and cosmic ray acceleration in MHD simulations

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in collaboration with

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Supernova remnant simulations

Astrophysical shocks

Introduction Injection algorithm Supernova remnant simulations



solar system shocks $\sim R_{\odot}$ coronal mass ejection (SOHO)



interstellar shocks $\sim 20~pc$ supernova 1006 (CXC/Hughes)



cluster shocks $\sim 2~\text{Mpc}$ giant radio relic (van Weeren)

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Astrophysical shocks

Astrophysical collisionless shocks can:

- accelerate particles (electrons and ions) \rightarrow cosmic rays (CRs)
- amplify magnetic fields (or generate them from scratch)



solar system shocks $\sim R_{\odot}$ coronal mass ejection (SOHO)



interstellar shocks $\sim 20~pc$ supernova 1006 (CXC/Hughes)



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Supernova remnant simulations

Astrophysical shocks

Astrophysical collisionless shocks can:

- accelerate particles (electrons and ions) \rightarrow cosmic rays (CRs)
- amplify magnetic fields (or generate them from scratch)
- \Rightarrow non-thermal emission (radio to gamma rays)
- \Rightarrow cosmic ray feedback in galaxies and galaxy clusters



solar system shocks $\sim R_{\odot}$ coronal mass ejection (SOHO)



interstellar shocks \sim 20 pc supernova 1006 (CXC/Hughes)



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Unstructured moving-mesh code AREPO (Springel 2010)



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Shock finder





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Shock finder



Voronoi cells belong to shock zone if

- $\nabla \cdot \mathbf{v} < 0$ (converging flow)
- $\nabla T \cdot \nabla \rho > 0$ (filtering out tangential discontinuities)
- $\mathcal{M}_1 > \mathcal{M}_{min}$ (safeguard against numerical noise)



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Shock finder and CR acceleration



CR acceleration:

• shock surface: cell with most converging flow



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Shock finder and CR acceleration



CR acceleration:

- shock surface: cell with most converging flow
- collect pre- and post-shock energy at shock surface $\Rightarrow E_{diss}$
- inject $\Delta E_{cr} = \zeta(\mathcal{M}_1, \theta) E_{diss}$ to shock and 1st post-shock cell



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Shock finder and CR acceleration

Comparing simulations to exact solutions that include CR acceleration



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Shock finder and CR acceleration



CP, Pakmor, Schaal, Simpson, Springel (2017)



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Shock finder and CR acceleration



CP, Pakmor, Schaal, Simpson, Springel (2017)

CR acceleration:

● shock surface: cell with most converging flow along ∇7



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Shock finder and CR acceleration



CP, Pakmor, Schaal, Simpson, Springel (2017)

CR acceleration:

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Shock finder and CR acceleration



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- shock surface: cell with most converging flow along ∇7
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Sedov explosion

density



Supernova remnant simulations



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CP, Pakmor, Schaal, Simpson, Springel (2017)

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Sedov explosion with CR acceleration

density

specific cosmic ray energy

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Sedov explosion with CR acceleration



CP, Pakmor, Schaal, Simpson, Springel (2017)

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MHD setup

Protons and hadronic emission Electrons and leptonic emission

Global MHD simulations of SNRs with CR physics



 detect and characterize shocks and jump conditions on the fly

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Mach number finder with CRs

CP+ (2017)



MHD setup

Protons and hadronic emission Electrons and leptonic emission

Global MHD simulations of SNRs with CR physics



- detect and characterize shocks and jump conditions on the fly
- measure Mach number \mathcal{M} and magnetic obliquity θ_B

obliquity-dep. acceleration efficiency

Pais, CP+ (2018) based on hybrid PIC sim.'s by Caprioli & Spitkovsky (2015)



MHD setup

Protons and hadronic emission Electrons and leptonic emission

Global MHD simulations of SNRs with CR physics



simulated TeV gamma-ray map

Pais & CP (2020)

- detect and characterize shocks and jump conditions on the fly
- measure Mach number \mathcal{M} and magnetic obliquity θ_B
- inject and transport CR protons
 ⇒ dynamical back reaction on gas flow, hadronic emission



MHD setup

Protons and hadronic emission Electrons and leptonic emission

Global MHD simulations of SNRs with CR physics



simulated gamma-ray spectrum

Winner, CP+ (2019, 2020)

- detect and characterize shocks and jump conditions on the fly
- measure Mach number M and magnetic obliquity θ_B
- inject and transport CR protons
 ⇒ dynamical back reaction on gas flow, hadronic emission
- inject and transport CR electrons
- calculate non-thermal radio, X-ray, γ-ray emission



MHD setup Protons and hadronic emission Electrons and leptonic emission

Hadronic TeV γ rays: SN 1006



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Protons and hadronic emission

Hadronic TeV γ rays: SN 1006

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Hadronic TeV γ rays: Vela Jr. and RXJ 1713



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TeV γ rays from shell-type supernova remnants

Varying magnetic coherence scale in simulations of SN 1006 and Vela Junior





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MHD setup Protons and hadronic emission Electrons and leptonic emission

TeV γ rays from shell-type supernova remnants

Varying magnetic coherence scale in simulations of SN 1006 and Vela Junior



Pais, CP+ (2020)

 \Rightarrow Correlation structure of patchy TeV γ -rays constrains magnetic coherence scale in ISM:

SN 1006: $\lambda_B > 200^{+80}_{-10}$ pc

Vela Junior:
$$\lambda_B = 13^{+13}_{-4.3} \text{ pc}$$



Shocks and cosmic ray acceleration

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CREST - Cosmic Ray Electron Spectra evolved in Time



CREST code (Winner, CP+ 2019)

- post-processing MHD simulations
- on Lagrangian particles
 - adiabatic processes
 - Coulomb and radiative losses
 - Fermi-I (re-)acceleration
 - Fermi-II reacceleration
 - secondary electrons

Link to observations

- radio synchrotron
- inverse Compton (IC) γ-ray



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Sedov-Taylor blast wave: spectral evolution



Winner, CP+ (2019)

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$$E_0 = 10^{51} \, \mathrm{erg}, \; n_{\mathrm{gas}} = 1 \, \mathrm{cm}^{-3}, \; T_0 = 10^4 \, \mathrm{K}, \; B = 1 \, \mathrm{\mu G}$$

MHD setup Protons and hadronic emission Electrons and leptonic emission

SN 1006: CR electron acceleration models



• different obliquity dependent electron acceleration efficiencies:

- 1. preferred quasi-perpendicular acceleration (previous PIC)
- 2. constant acceleration efficiency (a straw man's model)
- 3. preferred quasi-parallel acceleration (like CR protons)



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CR electron acceleration: quasi-perpendicular shocks





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CR electron acceleration: constant efficiency



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CR electron acceleration: quasi-parallel shocks





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SN 1006: multi-frequency spectrum



Winner, CP+ (2020)

quasi-parallel acceleration model fits multi-frequency spectrum



MHD setup Protons and hadronic emission Electrons and leptonic emission

SN 1006: multi-frequency spectrum



Winner, CP+ (2020)

- quasi-parallel acceleration model fits multi-frequency spectrum
- GeV regime: leptonic inverse Compton dominates
- TeV regime: hadronic pion decay



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SN 1006: maps of γ -ray components at E > 500 GeV



Winner, CP+ (2020)

- hadronic pion decay emission dominant at shock rim
- leptonic IC emission has contributions from SNR interior



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SN 1006: magnetic field amplification models

Magnetic amplification due to a turbulent dynamo and Bell's instability



Winner, CP+ (2020)

magnetic field strength in a slice through the simulated SNRs



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SN 1006: magnetic field amplification models

Magnetic amplification due to a turbulent dynamo and Bell's instability



Winner, CP+ (2020)

- magnetic field strength in a slice through the simulated SNRs
- left: effect of turbulent amplification only, maximum realized at quasi-perpendicular shock, adiabatic cooling inside the SNR
- middle: effect of Bell amplification only, f_{Bell} follows obliquity dependence of CR proton efficiency
- right: sum of both, turbulent and Bell amplification



MHD setup Protons and hadronic emission Electrons and leptonic emission

Constraining the volume-filling, turbulent **B** field



 multi-frequency spectra: synchrotron (radio + X-rays) and IC and hadronic γ-ray emission

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Constraining the volume-filling, turbulent **B** field



- multi-frequency spectra: synchrotron (radio + X-rays) and IC and hadronic γ-ray emission
- strong, volume-filling *B* field (≈ 35 µG) required to suppress IC γ-ray component and to match steep X-ray spectrum



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SN 1006: best-fit multi-frequency spectrum



Winner, CP+ (2020)

parameter optimization of magnetic amplification processes



MHD setup Protons and hadronic emission Electrons and leptonic emission

SN 1006: best-fit multi-frequency spectrum



Winner, CP+ (2020)

- parameter optimization of magnetic amplification processes
- strong (≈ 35 µG) volume-filling *B* field (turbulent dynamo): lower *B* field excluded by IC component
- Bell-amplification factor f_{Bell} 10 20 weakly constrained





Conclusions for CR hydrodynamics at SNRs

CR hydrodynamics with kinetic plasma physics:

- Shock finder enables CR acceleration in MHD simulations
- CR proton transport in MHD enables dynamic backreaction
- CR electron spectral transport (CREST): multi-frequency spectra and emission maps



Conclusions for CR hydrodynamics at SNRs

CR hydrodynamics with kinetic plasma physics:

- Shock finder enables CR acceleration in MHD simulations
- CR proton transport in MHD enables dynamic backreaction
- CR electron spectral transport (CREST): multi-frequency spectra and emission maps
- CR acceleration constraints by MHD models:
 - TeV shell-type SNRs probe magnetic coherence scale in ISM
 - hybrid-PIC simulations of p⁺ acceleration agree with global SNR simulations
 - global SNR simulations imply preferred quasi-parallel e⁻ acceleration: new intermediate instability enables e⁻ (pre-)acceleration



MHD setup Protons and hadronic emission Electrons and leptonic emission

PICOGAL: From Plasma KInetics to COsmological GALaxy Formation





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Shocks and cosmic ray acceleration

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Literature for the talk

Cosmic ray hydrodynamics and shock acceleration:

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